

# Group Oriented Attribute-based Encryption Scheme from Lattices with Shamir's Secret Sharing scheme

*Maharage Nisansala Sevewandi Perera<sup>1</sup>,  
Toru Nakamura<sup>2</sup>, Takashi Matsunaka<sup>1</sup>,  
Hiroyuki Yokoyama<sup>1</sup>, and Kouichi Sakurai<sup>3</sup>*

1: Advanced Telecommunications Research Institute International (ATR), Kyoto, Japan  
2: KDDI Research, Inc., Saitama, Japan  
3: Kyushu University, Fukuoka, Japan

NSS 2023 – Canterbury, UK  
15<sup>th</sup> Aug., 2023

# Abstract

---

We construct Group Oriented (GO) Attribute-based Encryption (ABE) scheme (GO-ABE scheme) using the post-quantum cryptographic primitive lattices and employ Shamir's secret sharing scheme to satisfy GO-ABE requirements.

# Abstract

---

We construct Group Oriented (GO) Attribute-based Encryption (ABE) scheme (GO-ABE scheme) using the post-quantum cryptographic primitive lattices and employ Shamir's secret sharing scheme to satisfy GO-ABE requirements.

## Content

---

### Group Oriented Attribute-based Encryption

- Attribute-based Encryption (ABE) : KP-ABE and CP-ABE

- GO-ABE Scheme

- Requirement of GO-ABE

### Post-quantum construction of GO-ABE (our Goal)

- Post-quantum primitive – Lattices

- Need of Shamir's Secret Sharing Scheme

- Post- quantum (step by step) construction

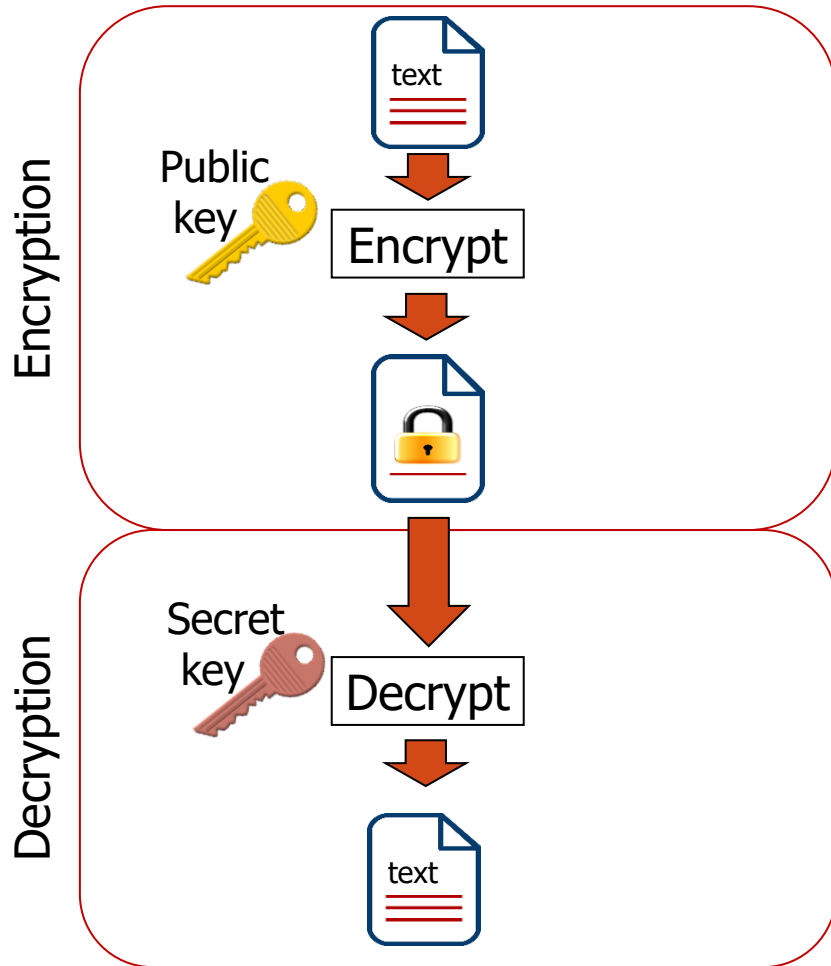
- Summary with Limitations

---

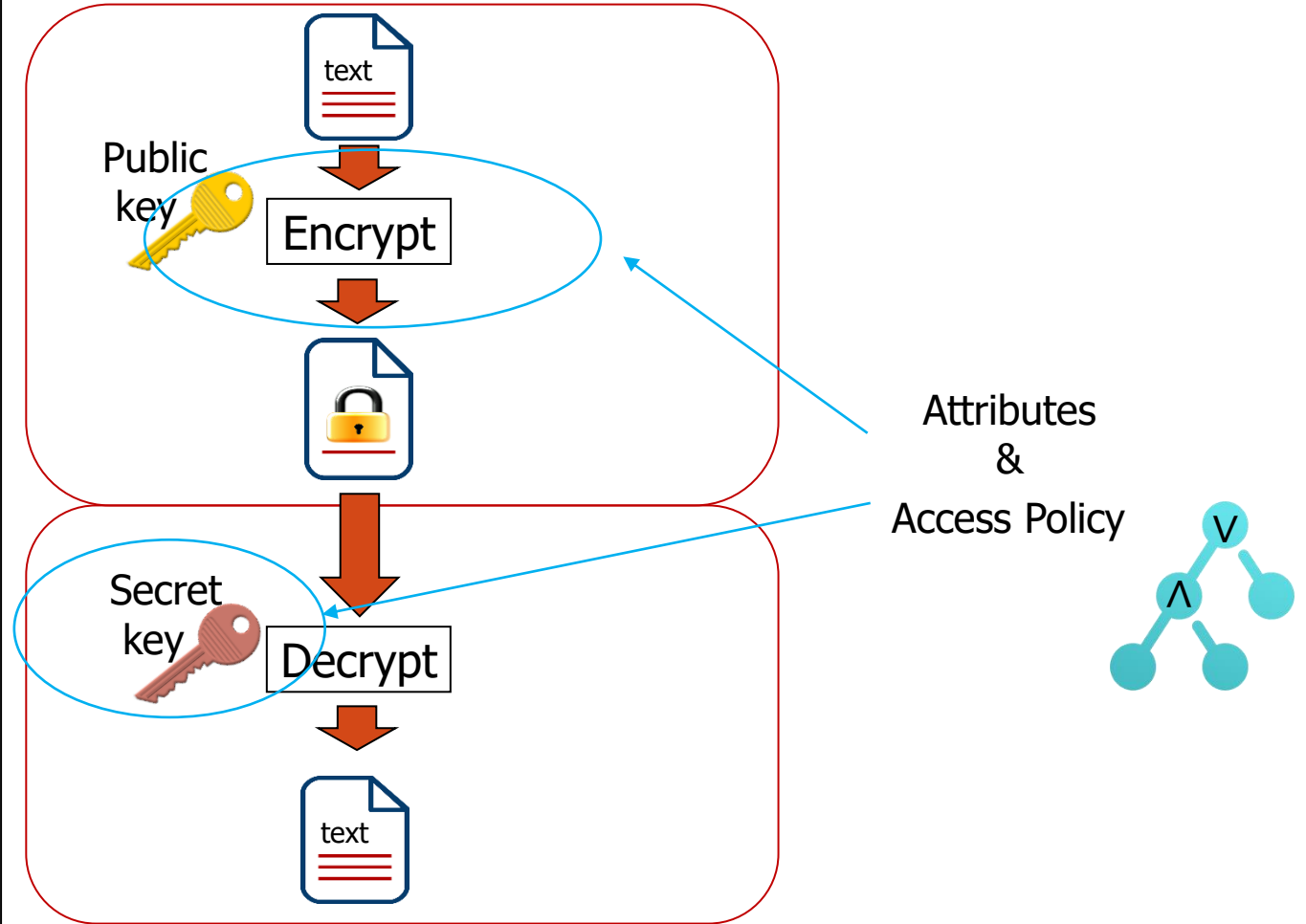
# **GROUP ORIENTED ATTRIBUTE BASED ENCRYPTION SCHEME**

# Attribute-based Encryption (ABE)

## Public-key Encryption (PKE)



## Attribute-based Encryption (ABE)



# ABE

## KP-ABE

## CP-ABE

**Key Policy ABE:**  
Ciphertext is associated to a attribute set; private key associated to a policy.  
Policy decides which data can be decrypted.

**Ciphertext Policy ABE:**  
Ciphertext is associated to a policy; private key associated to a attribute set.  
Policy decides who can decrypt the data.

Data 1:  
News: Celebrity  
Channel: Movies  
Place: Asia

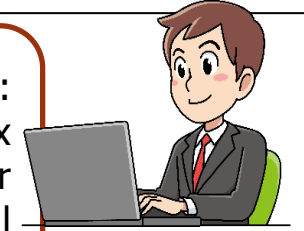
Data 2:  
News : Matches  
Channel: Sports  
Place: Japan

Data 3:  
News: Culture  
Channel: Cartoon  
Place: Europe

User 1:  
Name: Alex  
Position: Doctor  
Place: ABC Hospital

User 2:  
Name: Ann  
Position: Patient  
Place: Japan

User 3:  
Name: Charles  
Position: Clark  
Place: ABC Hospital



Sports

Patient

Doctor

Cultural Events

AND

AND

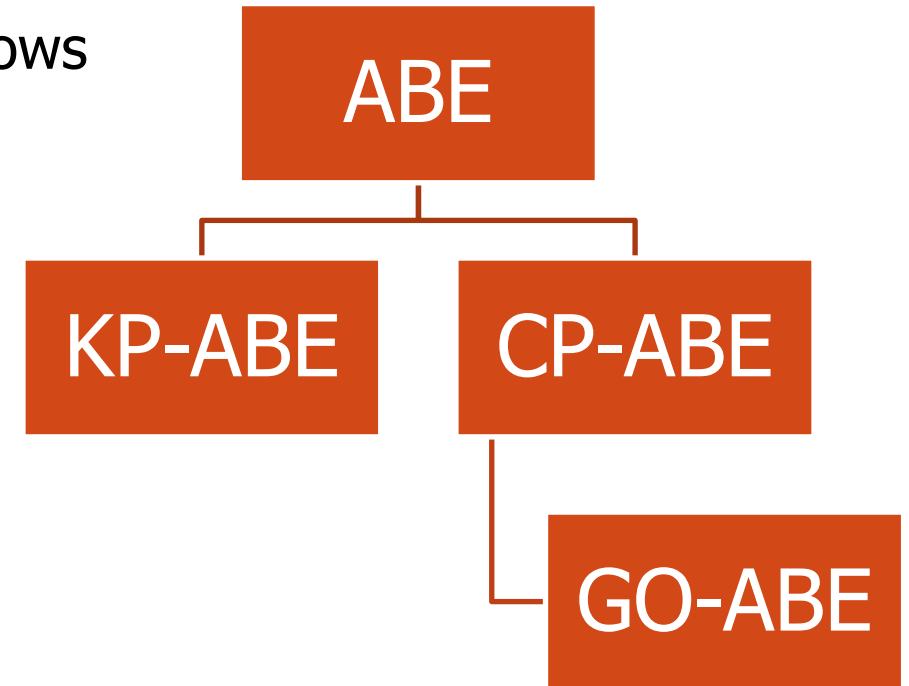
General Hospital

# GO-ABE [Li et al. 2015]

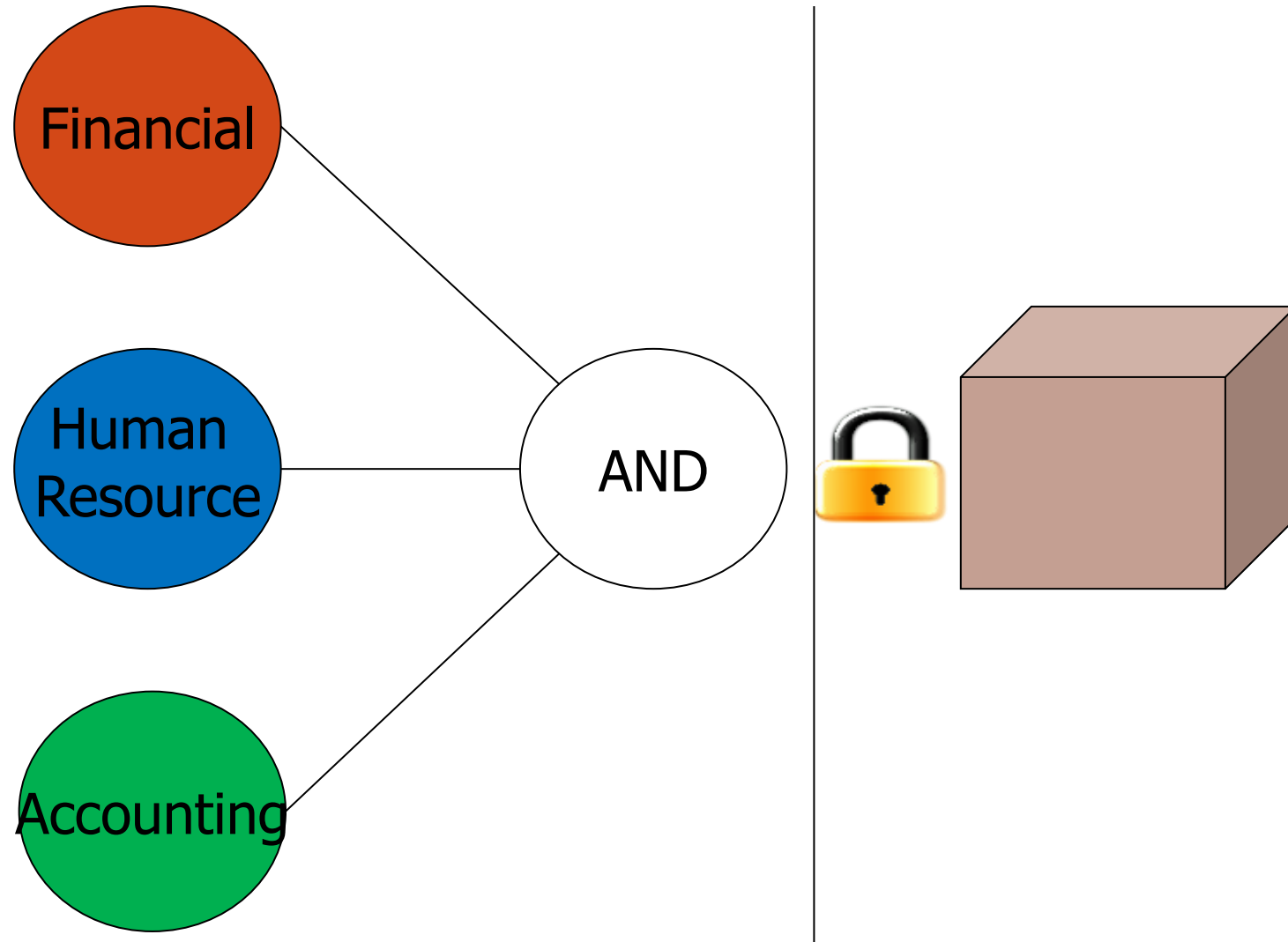
- Group Oriented Attribute-based Encryption (GO-ABE) was introduced by Li et al. in NSS2015
- Group Oriented Attribute-based Encryption (GO-ABE) allows
  - **Users** from the **Same Group**  
to cooperate to decrypt a ciphertext
  - **Without revealing** their **secret keys**

“Users from the same group are able to cooperate with each other to decrypt a ciphertext encrypted under a set of attributes  $\alpha$  such that a single user may not have enough attributes to match the attribute set  $\alpha$ ”

[Li et al. 2015].



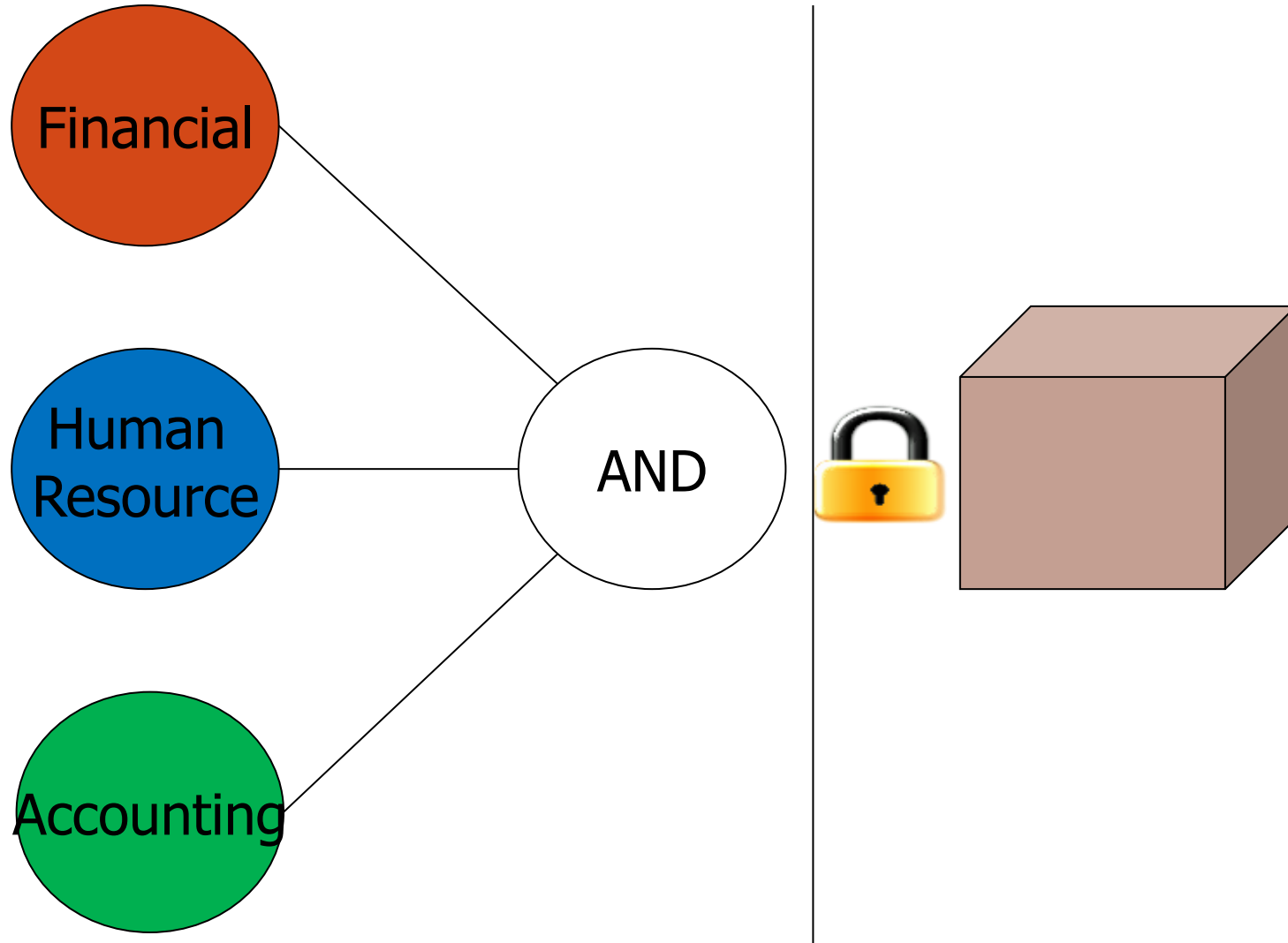
# Requirement of GO-ABE – Confidential Data Access



In a company structure, it is obvious requiring high level managers involvement from different departments to access company confidential data probably saved in the cloud.

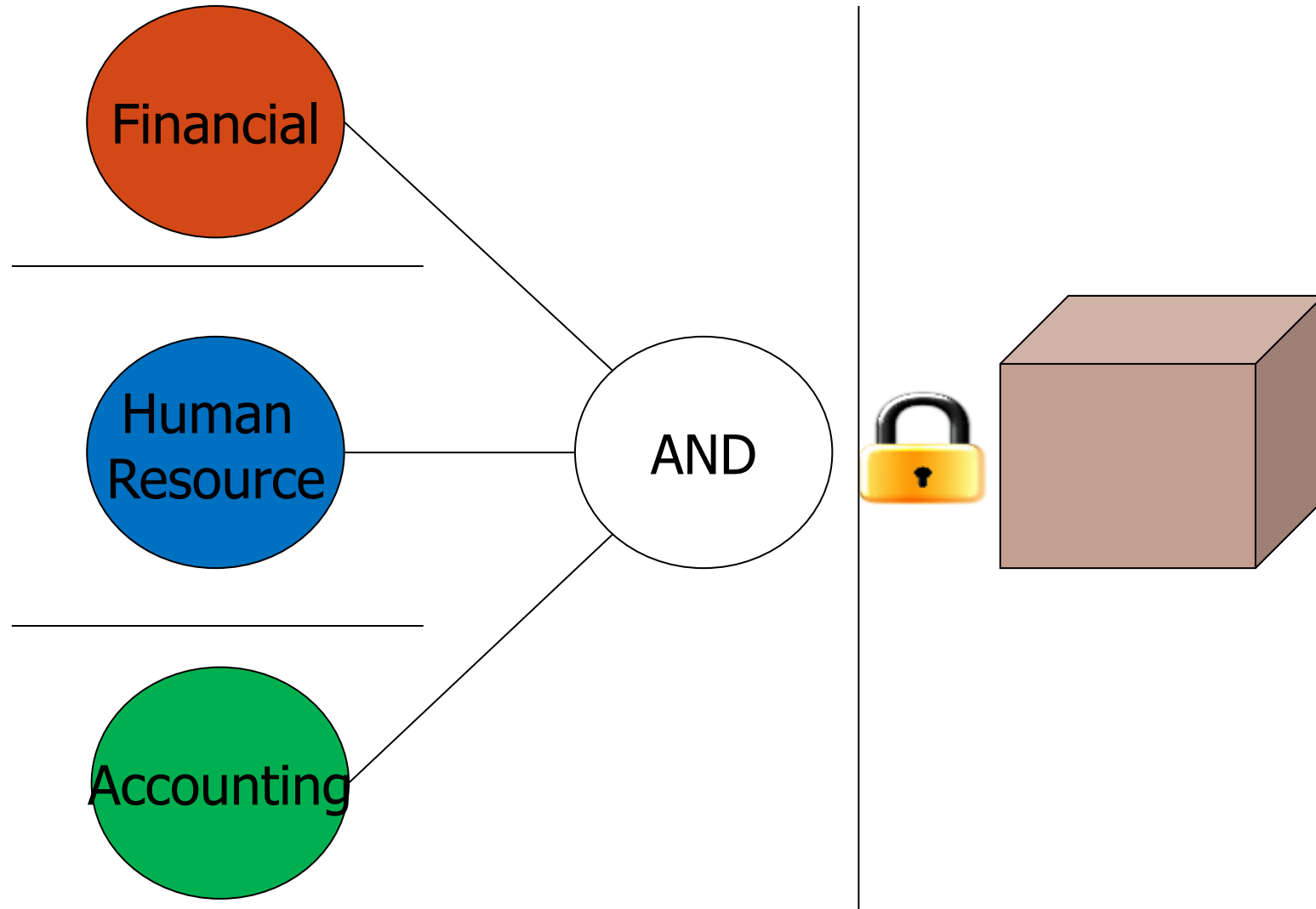


# Requirement of GO-ABE – Confidential Data Access



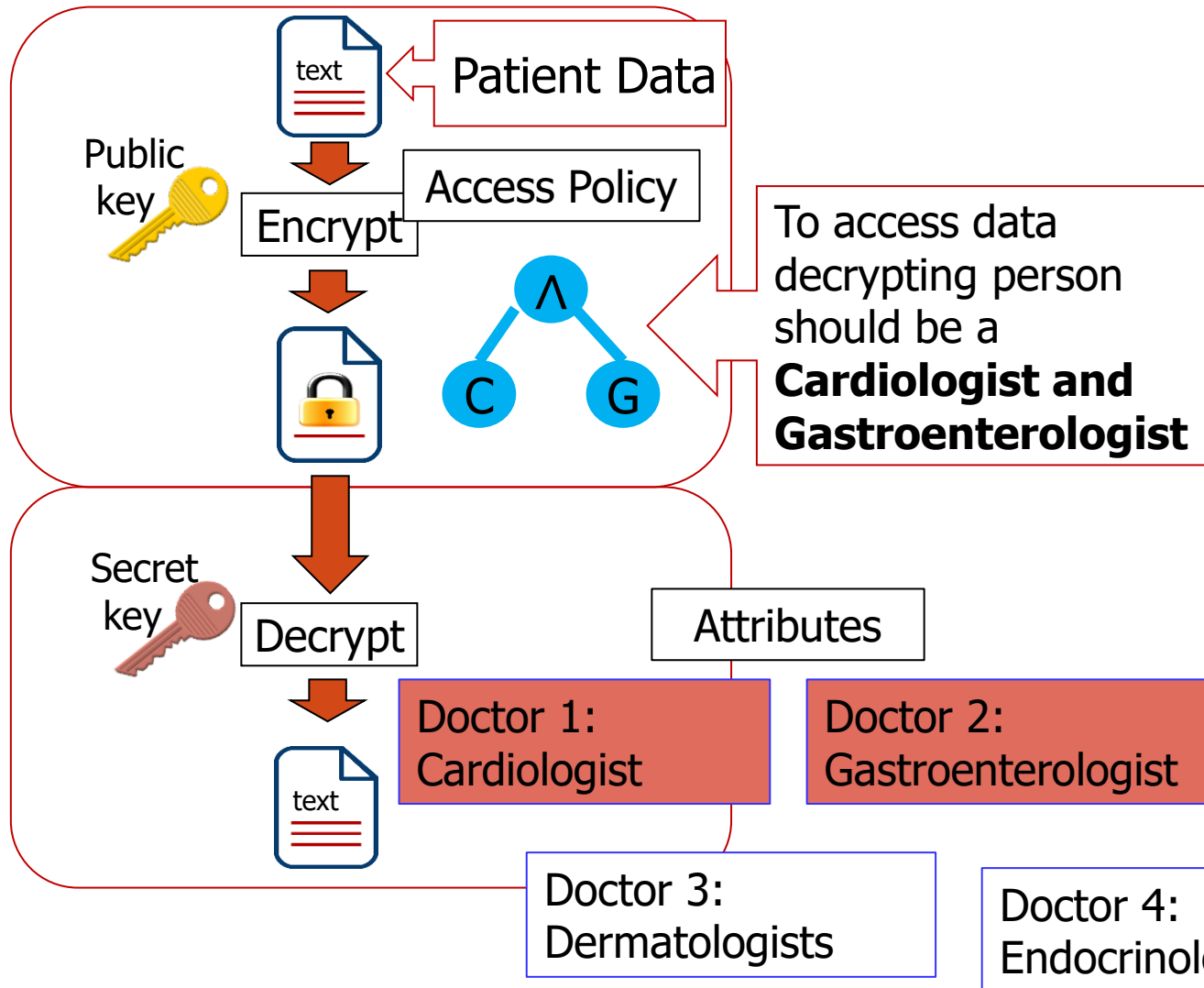
But CP-ABE allows a single party who possesses all the required attributes to access data. It is not practical because no manager may hold all the positions from different departments.

# Requirement of GO-ABE – Confidential Data Access



Allow managers from all required departments to collaborate for accessing data – which is the real requirement of company structure

# Requirement of GO-ABE – Access Patient Data [Li et al. 2015]



Doctor 1 (**Cardiologist**) and Doctor 2 (**Gastroenterologist**) collaborate

# GO-ABE [Li et al. 2015]

Algorithm	Input	Output
Setup	Security parameter $\lambda$	Public parameter <b>PK</b> Master secret key <b>MK</b>
Encryption	Public parameter <b>PK</b> Message $M$ Access Policy $\mathcal{W}$	Ciphertext $C$
KeyGen	Public parameter <b>PK</b> Master secret key <b>MK</b> Group id $g$ Attribute set $S$	Decryption Key $\mathbf{SK}_S^g$
Decryption	Ciphertext $C$ Public parameter <b>PK</b> Group id $g$	Message $M$

Cooperating user attribute sets:

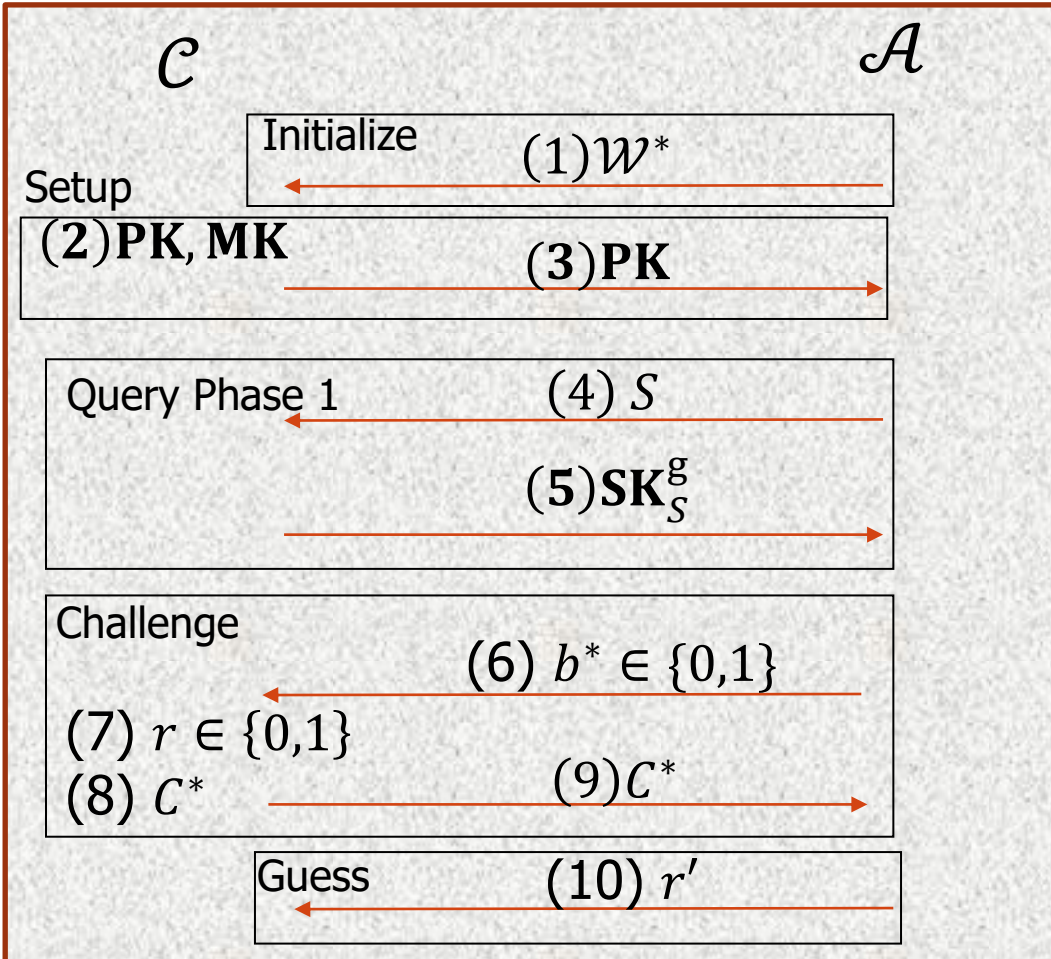
$$U = S_1 \cup S_2 \cup \dots \cup S_N$$

Decrypt if  $|\mathcal{W} \cap U| \geq t$ ,  
 $t$  is the threshold value

- Satisfies the selective set model security

# Selective Set-model Security

The adversary's goal is to determine which of the two messages is encrypted using the predefined attribute set  $\mathcal{W}^*$ .



$\mathcal{A}$  is an adversary against selective-set model anonymity.  $\mathcal{C}$  is a Challenger.

(1)  $\mathcal{A}$  sends the challenging access structure  $\mathcal{W}^*$ .

(2)  $\mathcal{C}$  creates  $\text{PK}$  and  $\text{MK}$

(3) Gives  $\text{PK}$  to  $\mathcal{A}$ .

(4)  $\mathcal{A}$  queries private keys for attribute set  $S \neq \mathcal{W}^*$  and

(5)  $\mathcal{C}$  replies with  $\text{SK}_S^g$  querying his own oracle.

(6)  $\mathcal{A}$  sends the message  $b^* \in \{0,1\}$ .

(7)  $\mathcal{C}$  selects a random  $r \in \{0,1\}$ .

(8) If  $r = 0$ ;  $c_1^*, c_2^*$  are honest values. Else selects randomly.

(9)  $\mathcal{C}$  outputs  $C^* = (\mathcal{W}^*, c_1^*, c_2^*)$

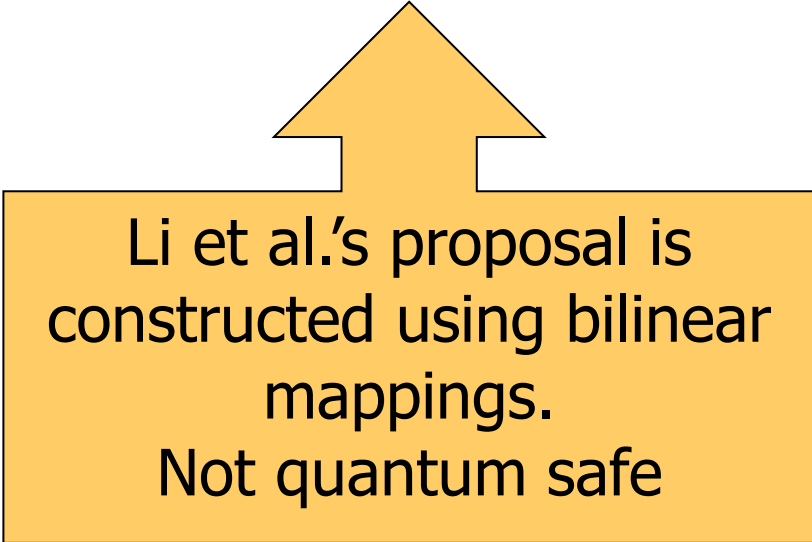
(10)  $\mathcal{A}$  sends  $r'$ .

If  $r' = r$  then  $\mathcal{A}$  wins.

# GO-ABE [Li et al. 2015]

- Group Oriented Attribute-based Encryption (GO-ABE) allows
  - **Users** from the **Same Group**  
to cooperate to decrypt a ciphertext
  - **Without revealing** their **secret keys**

Users from the same group are able to cooperate with each other to decrypt a ciphertext encrypted under a set of attributes  $\alpha$  such that a single user may not have enough attributes to match the attribute set  $\alpha$  [Li et al. 2015].



Li et al.'s proposal is  
constructed using bilinear  
mappings.  
Not quantum safe

# Our Goal

---

- Provide a quantum safe construction for the GO-ABE scheme
  - ▣ What are the supporting primitives / building blocks in our proposal
    - Lattice-based cryptography
    - Shamir's secret sharing scheme

---

# **GO-ABE SCHEME FROM LATTICES**



# Lattice-based Cryptography

- Is quantum safe because computational problems like Approximate Shortest Independent Vector Problem ( $SIVP_\lambda$ ) not broken (yet).
- We use Learning with error ( $LWE$ ) and Small Integer Solution ( $SIS$ ).
- $LWE$  asked to distinguish  $LWE$  samples from truly random samples
- $SIS$  asked to find small non-zero vector  $x$ , such that  $A \cdot x = 0 \pmod q$  and  $\|x\|_\infty \leq \beta$

LWE: Learning With Errors

$$\begin{pmatrix} A \end{pmatrix} \begin{pmatrix} x \end{pmatrix} + \begin{pmatrix} e \end{pmatrix} = \begin{pmatrix} z \end{pmatrix}$$

For given  $(A, z)$ , find  $(x, e)$

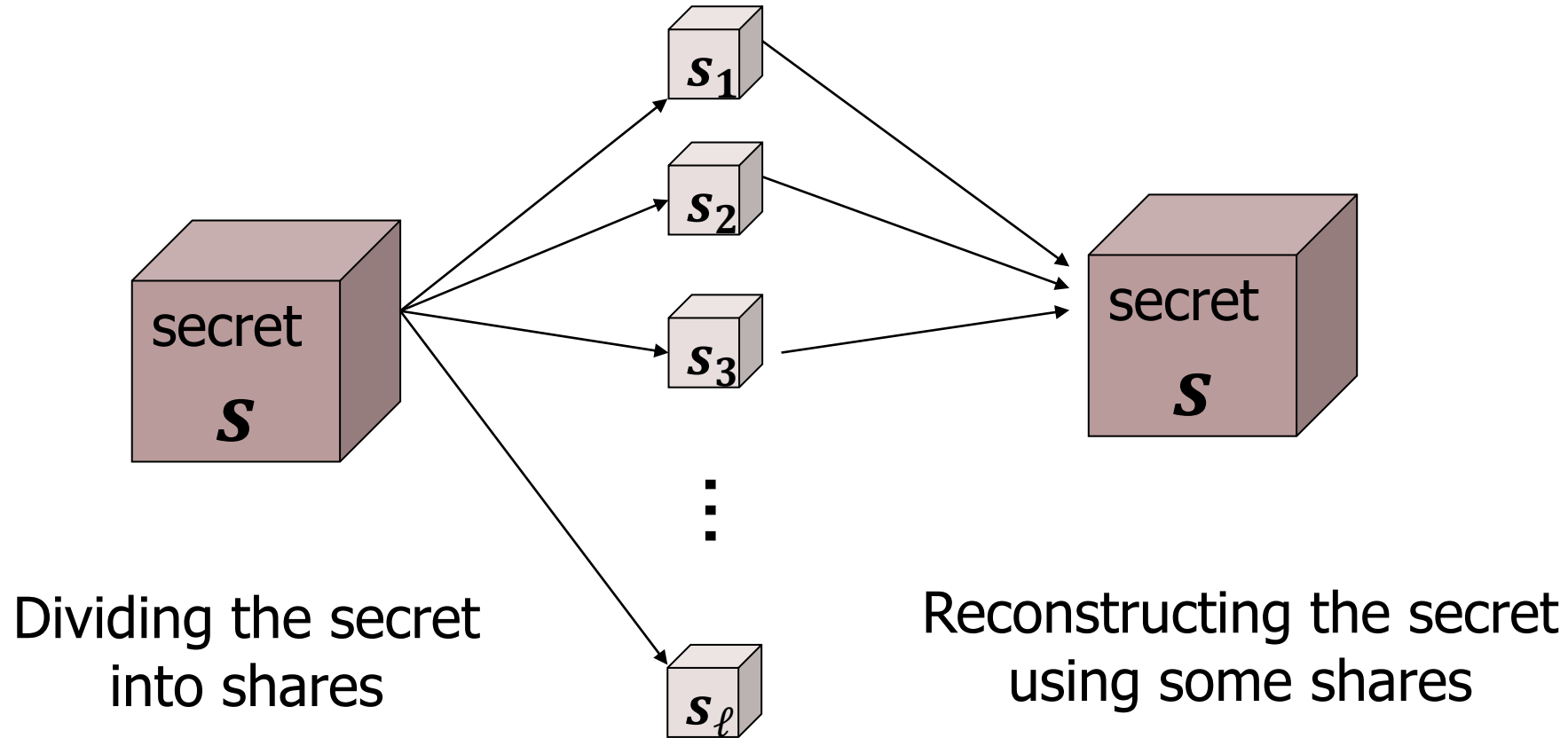
SIS: Short Integer Solution

$$\begin{pmatrix} A \end{pmatrix} \begin{pmatrix} x \end{pmatrix} = \begin{pmatrix} 0 \end{pmatrix} \pmod q$$

For given  $(A)$ , find non-zero vector  $(x)$

# Shamir's Secret Sharing (SSS) scheme

- A secret  $s$  is split into  $\ell$  shares; at least  $k$  shares should be combined to reconstruct the secret  $s$



# Why we use Shamir's Secret Sharing (SSS) scheme

GO-ABE Requirement:

Users should be from the same group  
Users should keep their attribute secret keys secure

# Why we use Shamir's Secret Sharing (SSS) scheme

GO-ABE Requirement:

Users should be from the same group  
Users should keep their attribute secret keys secure

SSS allows  $J$  shares of  $\ell$  shares to construct the origin.

In our construction,

Public key  $u = (u_1, u_2, \dots, u_n)$

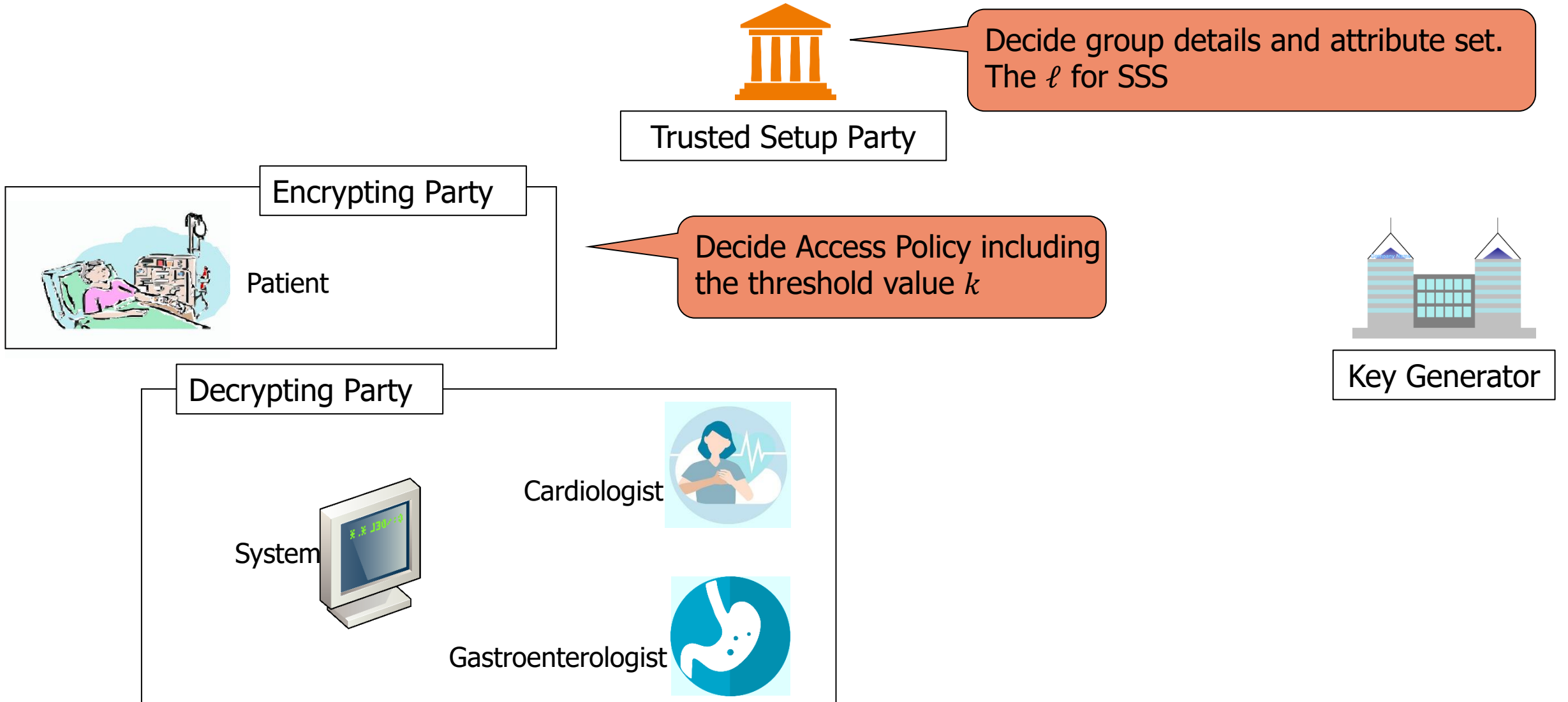
Share  $u$  among  $\ell$  shares, such that  $j$ -th share vector  $\hat{u}_j = (\hat{u}_{j,1}, \dots, \hat{u}_{j,n})$

The fractional Lagrangian coefficient  $L_j$  is calculated such that,  $u =$

$\sum_{j \in J} L_j$ , where  $J \subset [\ell]$

- ❖ Our proposal does not use SSS to reconstruct a secret; use for proving the users are from the same group.
- ❖ Shares are used to generate secret keys of individual users.

# Our Proposal: GO-ABE scheme construction from Lattices



# Our Proposal: GO-ABE scheme construction from Lattices



Trusted Setup Party

Encrypting Party

Let

each group has an id  $g$  and has unique group public key ( $\mathbf{GPK} = (\mathbf{G}, \mathbf{G}_0, \mathbf{G}_1, \mathbf{g})$ ).  
and a secret key ( $\mathbf{GSK} = \mathbf{T}$ ) selected from  $(\mathbf{G}, \mathbf{T}_{\mathbf{G}}) \leftarrow \text{TrapGen}(n, m, q)$  and  
 $\mathbf{G}_0, \mathbf{G}_1 \in \mathbb{Z}_q^{m \times n}$  and  $\mathbf{g} \in \mathbb{Z}_q^n$  randomly.

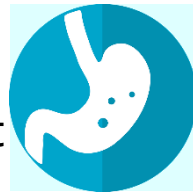
System



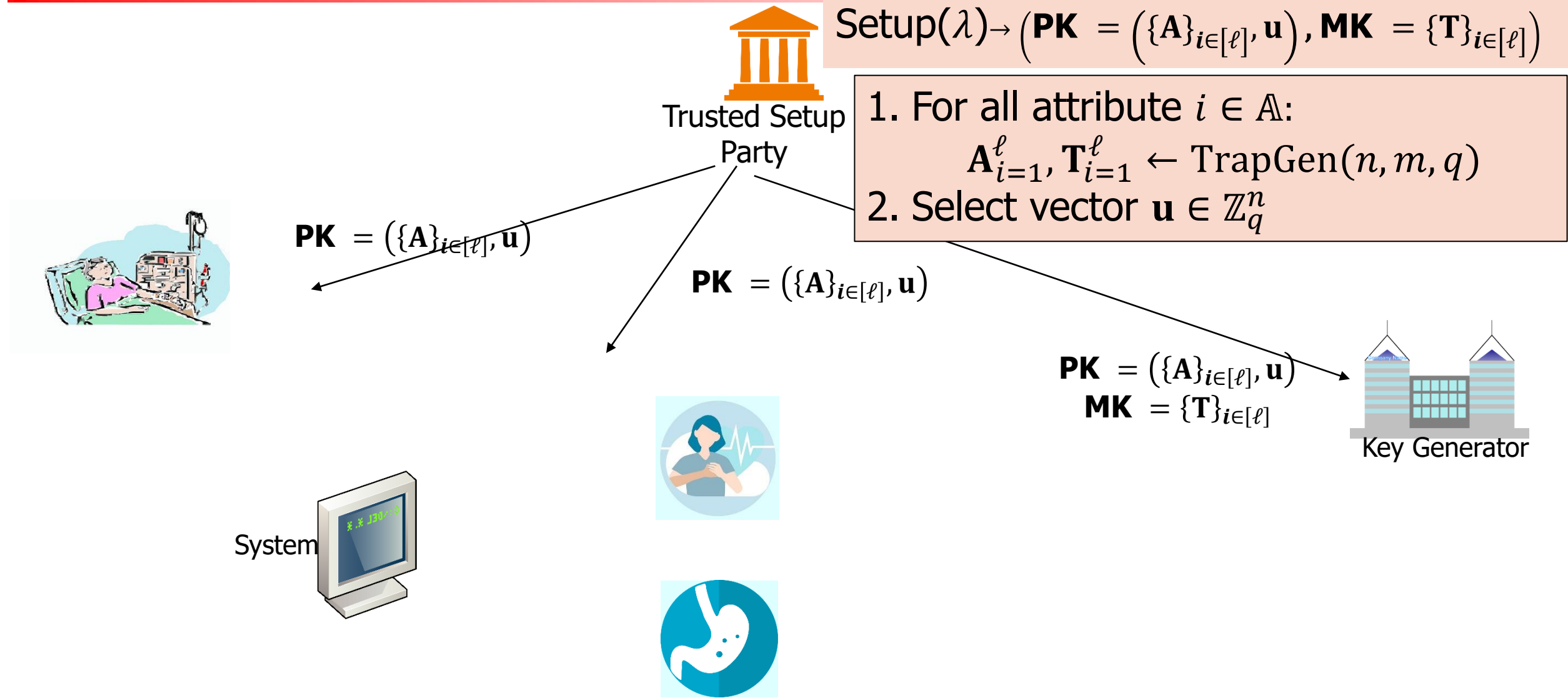
Cardiologist



Gastroenterologist



# Our Proposal: GO-ABE scheme construction from Lattices



# Our Proposal: GO-ABE scheme construction from Lattices

Encrypt(**PK**,  $M$ ,  $\mathcal{W}$ )  $\rightarrow$  ( $C = c_1, c_2$ )

1. Let  $D \stackrel{\text{def}}{=} (\ell!)^2$
2. Select  $\mathbf{s} \in \mathbb{Z}_q^n$ , for  $i \in [w]$ :  $\mathbf{e}_i \in \mathbb{Z}_q^m$ , and  $e \in \mathbb{Z}_q$
3.  $c_1 = \mathbf{A}_i^T \mathbf{s} + D \mathbf{e}_i$  for  $i \in [w]$ ,  
 $c_2 = \mathbf{u}^T \mathbf{s} + D e + M \lfloor q/2 \rfloor$

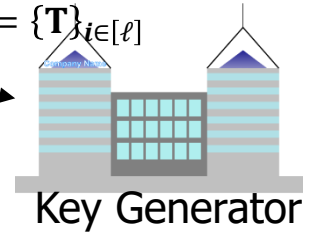


Trusted Setup Party

Setup( $\lambda$ )  $\rightarrow$  (**PK** =  $(\{\mathbf{A}\}_{i \in [\ell]}, \mathbf{u})$ , **MK** =  $\{\mathbf{T}\}_{i \in [\ell]}$ )

1. For all attribute  $i \in \mathbb{A}$ :  
 $\mathbf{A}_{i=1}^\ell, \mathbf{T}_{i=1}^\ell \leftarrow \text{TrapGen}(n, m, q)$
2. Select vector  $\mathbf{u} \in \mathbb{Z}_q^n$

**PK** =  $(\{\mathbf{A}\}_{i \in [\ell]}, \mathbf{u})$   
**MK** =  $\{\mathbf{T}\}_{i \in [\ell]}$



**PK** =  $(\{\mathbf{A}\}_{i \in [\ell]}, \mathbf{u})$



**PK** =  $(\{\mathbf{A}\}_{i \in [\ell]}, \mathbf{u})$





# Our Proposal: GO-ABE scheme construction from Lattices

Encrypt( $\mathbf{PK}, M, \mathcal{W}$ )  $\rightarrow (C = c_1, c_2)$

1. Let  $D \stackrel{\text{def}}{=} (\ell!)^2$
2. Select  $\mathbf{s} \in \mathbb{Z}_q^n$ , for  $i \in [w]: \mathbf{e}_i \in \mathbb{Z}_q^m$ , and  $e \in \mathbb{Z}_q$
3.  $c_1 = \mathbf{A}_i^T \mathbf{s} + D\mathbf{e}_i$  for  $i \in [w]$ ,  
 $c_2 = \mathbf{u}^T \mathbf{s} + De + M \lfloor q/2 \rfloor$



Trusted Setup Party

Setup( $\lambda$ )  $\rightarrow (\mathbf{PK} = (\{\mathbf{A}\}_{i \in [\ell]}, \mathbf{u}), \mathbf{MK} = \{\mathbf{T}\}_{i \in [\ell]})$

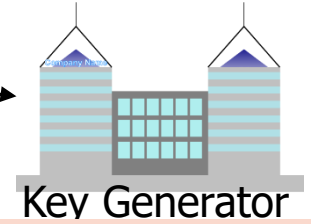
1. For all attribute  $i \in \mathbb{A}$ :  
 $\mathbf{A}_{i=1}^\ell, \mathbf{T}_{i=1}^\ell \leftarrow \text{TrapGen}(n, m, q)$
2. Select vector  $\mathbf{u} \in \mathbb{Z}_q^n$



$\mathbf{PK} = (\{\mathbf{A}\}_{i \in [\ell]}, \mathbf{u})$

$\mathbf{PK} = (\{\mathbf{A}\}_{i \in [\ell]}, \mathbf{u})$

$\mathbf{PK} = (\{\mathbf{A}\}_{i \in [\ell]}, \mathbf{u})$   
 $\mathbf{MK} = \{\mathbf{T}\}_{i \in [\ell]}$



Key Generator

KeyGen( $\mathbf{PK}, \mathbf{MK}, \mathbf{g}, S$ )  $\rightarrow (\mathbf{SK}_S^{\mathbf{g}} = ((\mathbf{x}_1^d, \dots, \mathbf{x}_S^d), \mathbf{d}))$

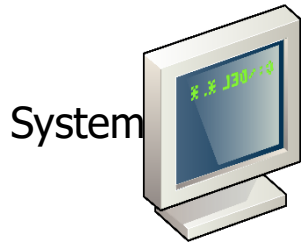
1. For a group:  $\mathbf{G}, \mathbf{T}_G \leftarrow \text{TrapGen}(n, m, q)$   
 $\mathbf{G}_0, \mathbf{G}_1 \in \mathbb{Z}_q^{m \times n}, \mathbf{g} \in \mathbb{Z}_q^n$   
 Set  $\mathbf{GPK} = (\mathbf{G}, \mathbf{G}_0, \mathbf{G}_1, \mathbf{g}), \mathbf{GSK} = \mathbf{T}_G$
2. User id  $d \in \mathbb{N}$
3. Use SSS on  $\mathbf{u}$ , such that  $\mathbf{u} = \sum_{j \in J} L_j \cdot \hat{\mathbf{u}}_j$
4. For  $i \in S$ :  
 $\mathbf{v}_i \leftarrow \text{SamplePre}(\mathbf{A}_i, \mathbf{T}_i, \hat{\mathbf{u}}_i - \mathbf{g}, \sigma); \mathbf{A}_i \cdot \mathbf{v}_i = \hat{\mathbf{u}}_i - \mathbf{g}$
5. Compute  $\mathbf{G}_d = [\mathbf{G} | \mathbf{G}_0 + d\mathbf{G}_1]$  and  
 $\mathbf{T}_d \leftarrow \text{ExtBasis}(\mathbf{T}_G, \mathbf{G}_d)$
6. For  $i \in S: \mathbf{x}_i^d \leftarrow \text{SamplePre}(\mathbf{G}_d, \mathbf{T}_d, \mathbf{v}_i, \sigma); \mathbf{G} \cdot \mathbf{x}_i^d = \mathbf{v}_i$



$\mathbf{SK}_{S=\text{Cardi}}^{\mathbf{g}}$



$\mathbf{SK}_{S=\text{Gas}}^{\mathbf{g}}$



System

# Our Proposal: GO-ABE scheme construction from Lattices

Encrypt( $\mathbf{PK}, M, \mathcal{W}$ )  $\rightarrow (C = c_1, c_2)$

1. Let  $D \stackrel{\text{def}}{=} (\ell!)^2$
2. Select  $\mathbf{s} \in \mathbb{Z}_q^n$ , for  $i \in [w]: \mathbf{e}_i \in \mathbb{Z}_q^m$ , and  $e \in \mathbb{Z}_q$
3.  $c_1 = \mathbf{A}_i^T \mathbf{s} + D\mathbf{e}_i$  for  $i \in [w]$ ,  
 $c_2 = \mathbf{u}^T \mathbf{s} + De + M\lfloor q/2 \rfloor$



Trusted Setup Party

Setup( $\lambda$ )  $\rightarrow (\mathbf{PK} = (\{\mathbf{A}\}_{i \in [\ell]}, \mathbf{u}), \mathbf{MK} = \{\mathbf{T}\}_{i \in [\ell]})$

1. For all attribute  $i \in \mathbb{A}$ :  
 $\mathbf{A}_{i=1}^\ell, \mathbf{T}_{i=1}^\ell \leftarrow \text{TrapGen}(n, m, q)$
2. Select vector  $\mathbf{u} \in \mathbb{Z}_q^n$

$\mathbf{PK} = (\{\mathbf{A}\}_{i \in [\ell]}, \mathbf{u})$

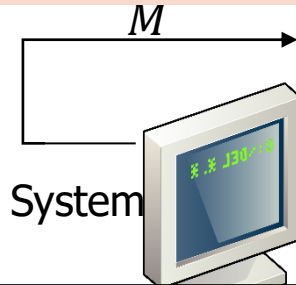
$\mathbf{PK} = (\{\mathbf{A}\}_{i \in [\ell]}, \mathbf{u})$

$\mathbf{PK} = (\{\mathbf{A}\}_{i \in [\ell]}, \mathbf{u})$   
 $\mathbf{MK} = \{\mathbf{T}\}_{i \in [\ell]}$



Key Generator

Decrypt( $\mathbf{PK}, C, \mathbf{g}$ )  $\rightarrow M$



KeyGen( $\mathbf{PK}, \mathbf{MK}, \mathbf{g}, S$ )  $\rightarrow (\mathbf{SK}_S^{\mathbf{g}} = ((x_1^d, \dots, x_s^d), \mathbf{d}))$

1. For a group:  
 $\mathbf{G}, \mathbf{T}_G \leftarrow \text{TrapGen}(n, m, q)$

Compute  $\mathbf{G}_d = [\mathbf{G} | \mathbf{G}_0 + d\mathbf{G}_1]$   
 publishes  $\mathbf{y}_i = (\mathbf{G}_d \cdot \mathbf{x}_i)$

$\mathbf{GSK} = \mathbf{T}_G$

$\mathbf{SK}_{S=\text{Cardi}}^{\mathbf{g}}$

$\mathbf{y}_C$

$\mathbf{y}_G$

$\mathbf{SK}_{S=\text{Gas}}^{\mathbf{g}}$

3. Use SSS on  $\mathbf{u}$ , such that  $\mathbf{u} = \sum_{j \in J} L_j \cdot \hat{\mathbf{u}}_j$

4. For  $i \in S$ :  
 $\mathbf{v}_i \leftarrow \text{SamplePre}(\mathbf{A}_i, \mathbf{T}_i, \hat{\mathbf{u}}_i - \mathbf{g}, \sigma); \mathbf{A}_i \cdot \mathbf{v}_i = \hat{\mathbf{u}}_i - \mathbf{g}$
5. Compute  $\mathbf{G}_d = [\mathbf{G} | \mathbf{G}_0 + d\mathbf{G}_1]$  and  
 $\mathbf{T}_d \leftarrow \text{ExtBasis}(\mathbf{T}_G, \mathbf{G}_d)$
6. For  $i \in S: \mathbf{x}_i^d \leftarrow \text{SamplePre}(\mathbf{G}_d, \mathbf{T}_d, \mathbf{v}_i, \sigma); \mathbf{G} \cdot \mathbf{x}_i^d = \mathbf{v}_i$

Calculate  $L_i; \sum_{i \in [k]} L_i \mathbf{A}_i \mathbf{y}_i = \mathbf{u} \text{ mod } q$   
 Compute  $r \leftarrow c_2 - ((k \times \mathbf{g})^T + \sum_{i \in [k]} L_i \mathbf{y}_i^T c_1)$   
 If  $|r| < \frac{q}{4}$ , output 0, else 1 as the message  $M$

# Our Proposal: GO-ABE scheme construction from Lattices

Encrypt( $\mathbf{PK}, M, \mathcal{W}$ )  $\rightarrow (C = c_1, c_2)$

1. Let  $D \stackrel{\text{def}}{=} (\ell!)^2$
2. Select  $\mathbf{s} \in \mathbb{Z}_q^n$ , for  $i \in [w]: \mathbf{e}_i \in \mathbb{Z}_q^m$ , and  $e \in \mathbb{Z}_q$
3.  $c_1 = \mathbf{A}_i^T \mathbf{s} + D \mathbf{e}_i$  for  $i \in [w]$ ,  
 $c_2 = \mathbf{u}^T \mathbf{s} + D e + M \lfloor q/2 \rfloor$



Trusted Setup Party

Setup( $\lambda$ )  $\rightarrow (\mathbf{PK} = (\{\mathbf{A}\}_{i \in [\ell]}, \mathbf{u}), \mathbf{MK} = \{\mathbf{T}\}_{i \in [\ell]})$

1. For all attribute  $i \in \mathbb{A}$ :  
 $\mathbf{A}_{i=1}^\ell, \mathbf{T}_{i=1}^\ell \leftarrow \text{TrapGen}(n, m, q)$
2. Select vector  $\mathbf{u} \in \mathbb{Z}_q^n$



$\mathbf{PK} = (\{\mathbf{A}\}_{i \in [\ell]}, \mathbf{u})$

$\mathbf{PK} = (\{\mathbf{A}\}_{i \in [\ell]}, \mathbf{u})$

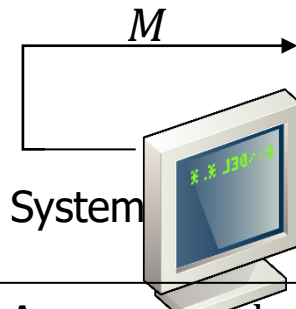
$\mathbf{PK} = (\{\mathbf{A}\}_{i \in [\ell]}, \mathbf{u})$   
 $\mathbf{MK} = \{\mathbf{T}\}_{i \in [\ell]}$



Key Generator

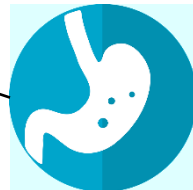
KeyGen( $\mathbf{PK}, \mathbf{MK}, \mathbf{g}, S$ )  $\rightarrow (\mathbf{SK}_S^g = ((x_1^d, \dots, x_s^d), \mathbf{d}))$

Decrypt( $\mathbf{PK}, C, \mathbf{g}$ )  $\rightarrow M$



$\mathbf{SK}_{S=\text{Cardi}}^g$

$\mathbf{y}_C$



$\mathbf{SK}_{S=\text{Gas}}^g$

$\mathbf{y}_G$

Compute  $\mathbf{G}_d = [\mathbf{G} | \mathbf{G}_0 + d \mathbf{G}_1]$   
 publishes  $\mathbf{y}_i = (\mathbf{G}_d \cdot \mathbf{x}_i)$

1. For a group:

$\mathbf{G}, \mathbf{T}_G \leftarrow \text{TrapGen}(n, m, q)$

$\mathbf{G}_0, \mathbf{G}_1 \in \mathbb{Z}_q^{m \times n}, \mathbf{g} \in \mathbb{Z}_q^n$

Set  $\mathbf{GPK} = (\mathbf{G}, \mathbf{G}_0, \mathbf{G}_1, \mathbf{g}), \mathbf{GSK} = \mathbf{T}_G$

2. User id  $d \in \mathbb{N}$

3. Use SSS on  $\mathbf{u}$ , such that  $\mathbf{u} = \sum_{j \in J} L_j \cdot \hat{\mathbf{u}}_j$

4. For  $i \in S$ :

$\mathbf{v}_i \leftarrow \text{SamplePre}(\mathbf{A}_i, \mathbf{T}_i, \hat{\mathbf{u}}_i - \mathbf{g}, \sigma); \mathbf{A}_i \cdot \mathbf{v}_i = \hat{\mathbf{u}}_i - \mathbf{g}$

5. Compute  $\mathbf{G}_d = [\mathbf{G} | \mathbf{G}_0 + d \mathbf{G}_1]$  and

$\mathbf{T}_d \leftarrow \text{ExtBasis}(\mathbf{T}_G, \mathbf{G}_d)$

6. For  $i \in S: \mathbf{x}_i^d \leftarrow \text{SamplePre}(\mathbf{G}_d, \mathbf{T}_d, \mathbf{v}_i, \sigma); \mathbf{G} \cdot \mathbf{x}_i^d = \mathbf{v}_i$

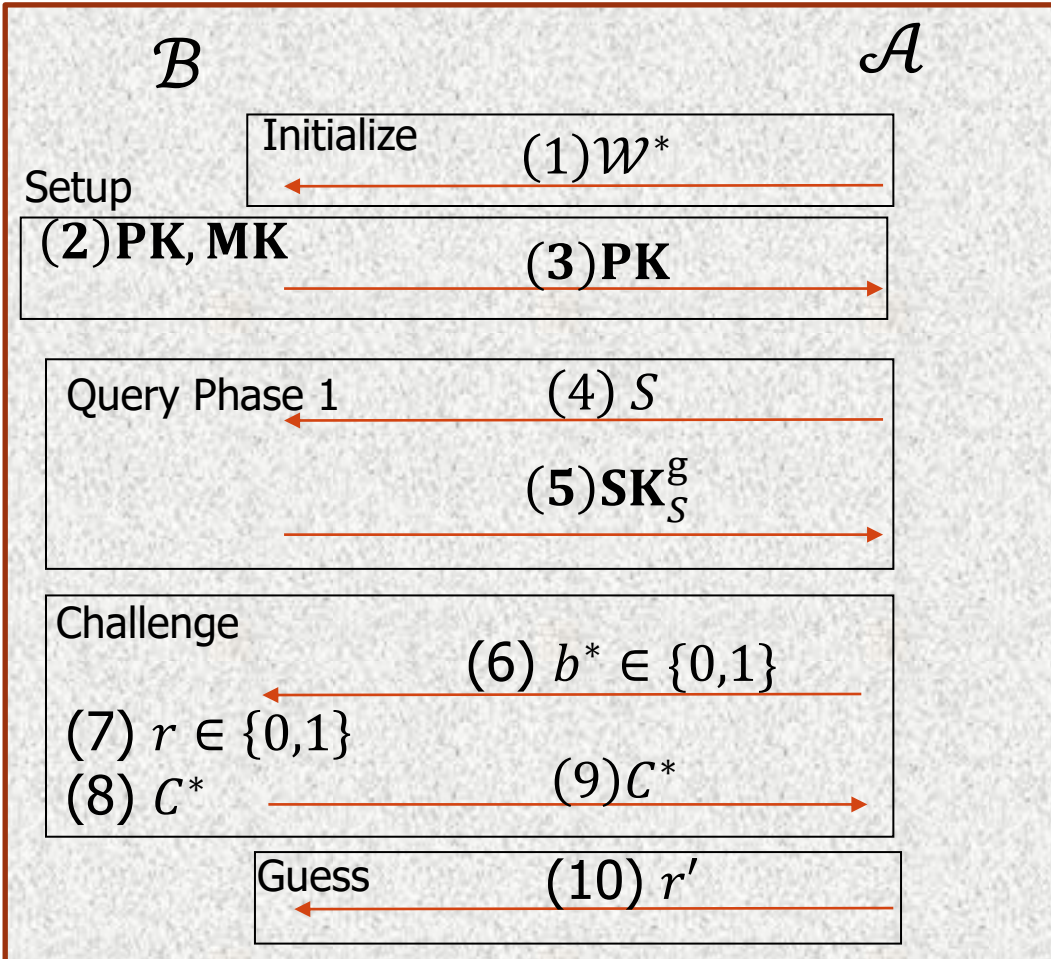
# Security Proof

- Based on the hardness of Decision-LWE problem we proved that Lattice-based construction of GO-ABE scheme provides ciphertext privacy in the Selective-Set model.
- Selective-Set model: The adversary declares the attribute set  $\mathcal{W}$  that he wishes to be challenged upon.

**Theorem 1.** *If there is an adversary  $\mathcal{A}$  with advantage  $> 0$  against the selective-set model for the GO-ABE scheme, then there exists a PPT algorithm  $\mathcal{B}$  that can solve the decision-LWE problem.*

# Selective Set-model Security

*Proof.* The simulator  $\mathcal{B}$  uses the adversary  $\mathcal{A}$  to distinguish LWE oracle  $\mathcal{O}$ . First  $\mathcal{B}$  queries the LWE oracle  $\mathcal{O}$  for  $(\ell m + 1)$  times and obtain LWE samples  $(a_k, b_k) \in \mathbb{Z}_q^n \times \mathbb{Z}_q$ , where  $k \in \{0, 1, 2, \dots, m\}$ . Then  $\mathcal{B}$  proceeds as below.



Initialize:  $\mathcal{A}$  announces to  $\mathcal{W}^*$  to  $\mathcal{B}$

Setup:  $\mathcal{B}$  selects LWE challenges

$\{(a_0, b_0), (a_i^1, b_i^1), (a_i^2, b_i^2), \dots, (a_i^m, b_i^m)\}_{i \in [\ell]}$  for public matrices  $\widehat{\mathbf{A}}_i$  and  $a_0$  as  $\mathbf{u}$

Phase 1:  $\mathcal{B}$  answers each private key query by selecting parameters from LWE

Challenge: When  $\mathcal{A}$  sends  $b^* \in \{0, 1\}$ ,  $\mathcal{B}$  uses  $\mathcal{W}^*$  and sets  $c_1 = (Db_i^1, Db_i^2, \dots, Db_i^m)$  for  $i \in [\ell]$

$c_2 = Da_0 + M_b \lfloor q/2 \rfloor$  if he wishes to generate  $C^*$ . That is  $r = 0$ . Otherwise he randomly selects values.

Guess:  $\mathcal{A}$  outputs  $b'$  If

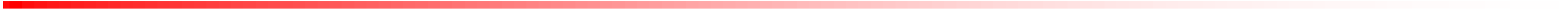
# Summary

---

- We present the Lattice based construction of GO-ABE scheme
- We employed Shamir's Secret Sharing Scheme to satisfy GO-ABE requirements
- **Limitations:**
  1. Efficiency is less in decryption because need to collect users' shares; however, this is reasonable fulfilling practical applications like access company confidential data  
-----
  2. Only AND-gets on multivalued attributes are considered; not complex access policies
  3. There is no tracing mechanism to track cooperated users
  4. The cooperating situation is not controlled
  5. Issues may occur due to the use of SSS:  
Ex: If any structural change happens like introducing new attributes, need recreate all the keys

Thank you for Listening

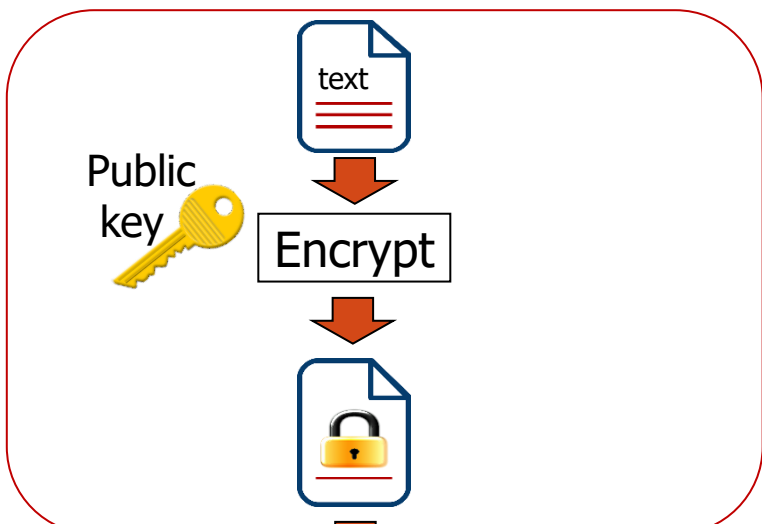
perera.nisansala@atr.jp



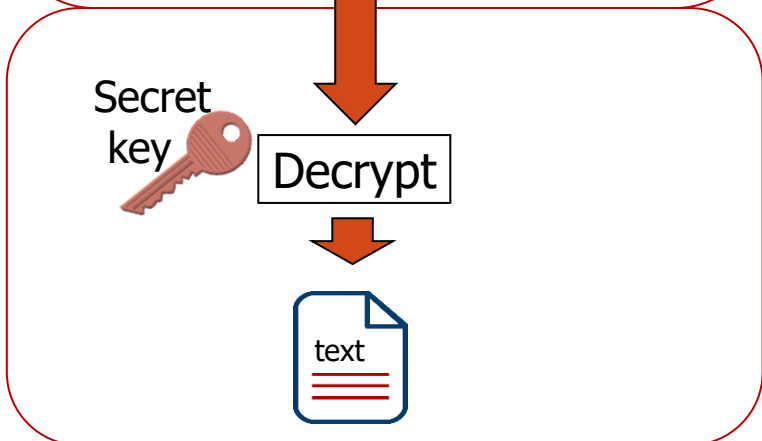
# Attribute-based Encryption (ABE)

## Public-key Encryption (PKE) 公開鍵暗号

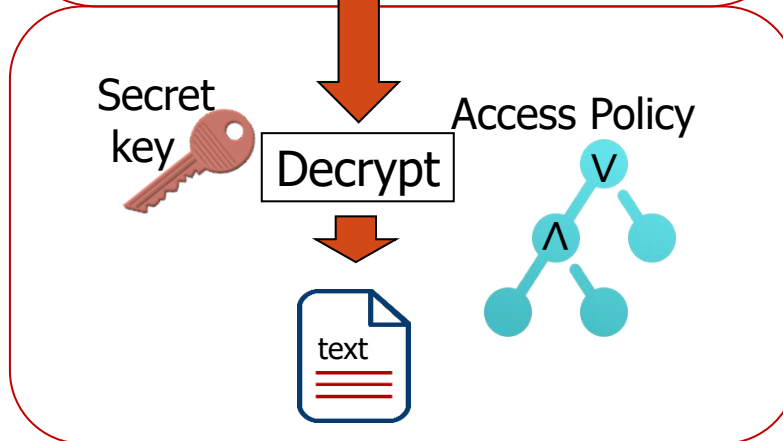
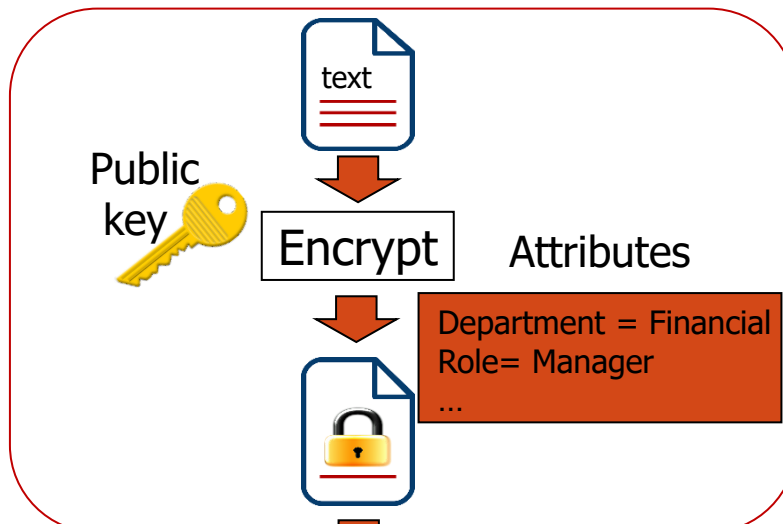
Encryption



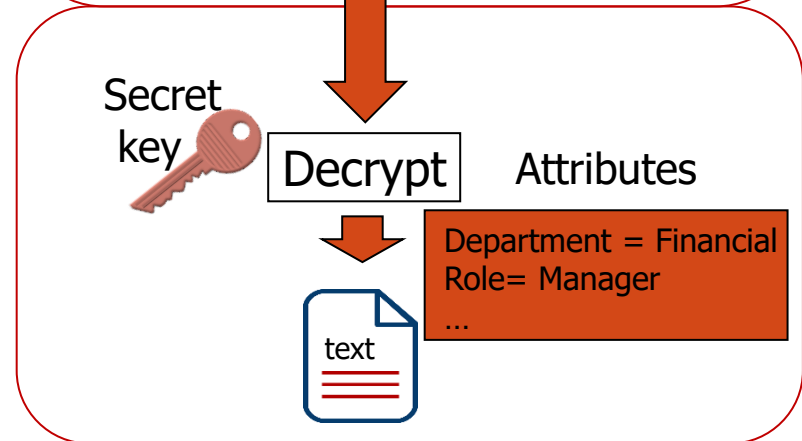
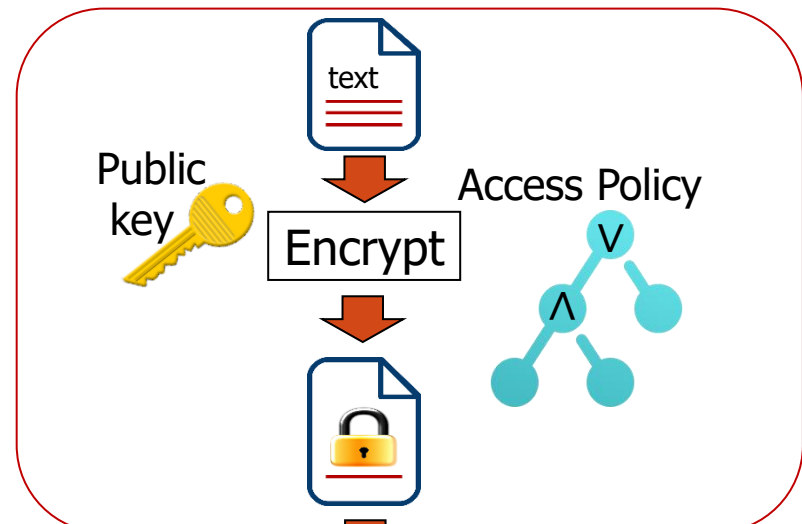
Decryption



## Key-Policy Attribute-based Encryption (KP-ABE)

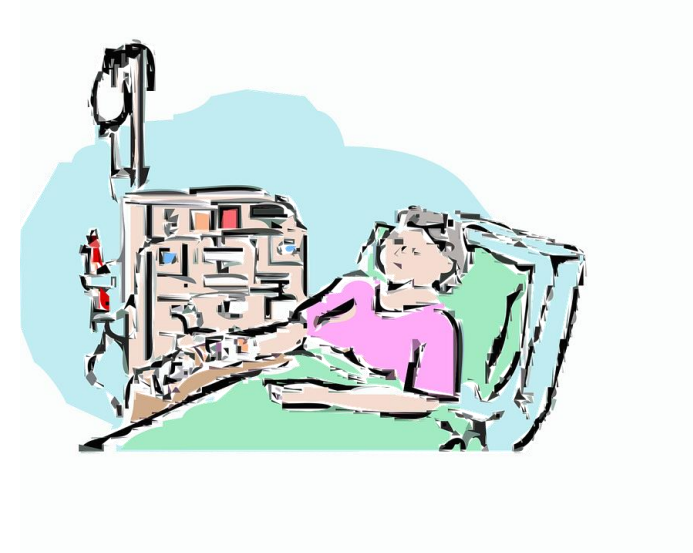
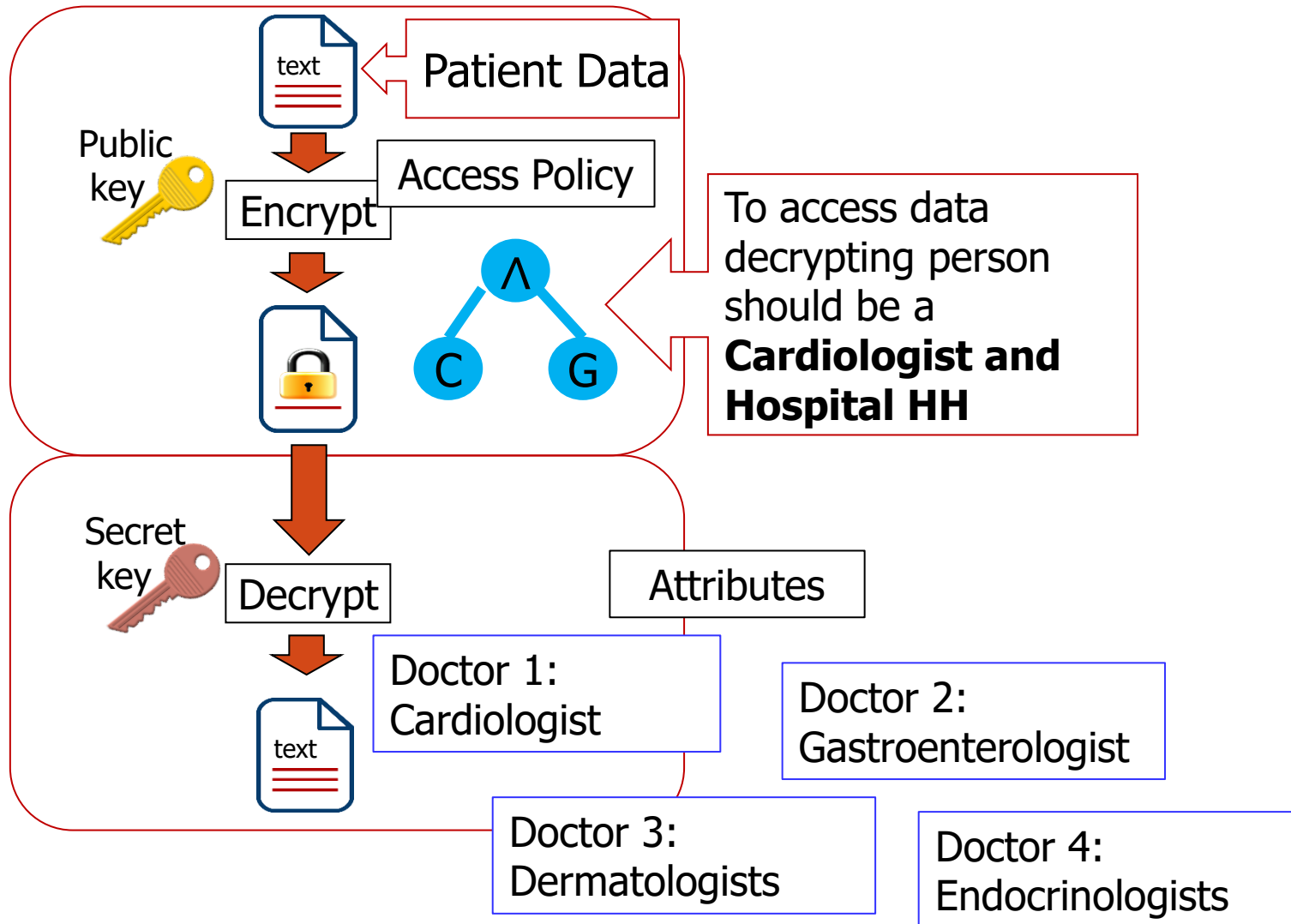


## Ciphertext-Policy Attribute-based Encryption (CP-ABE)

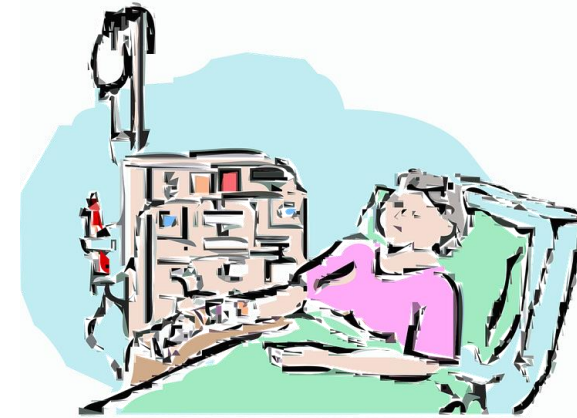
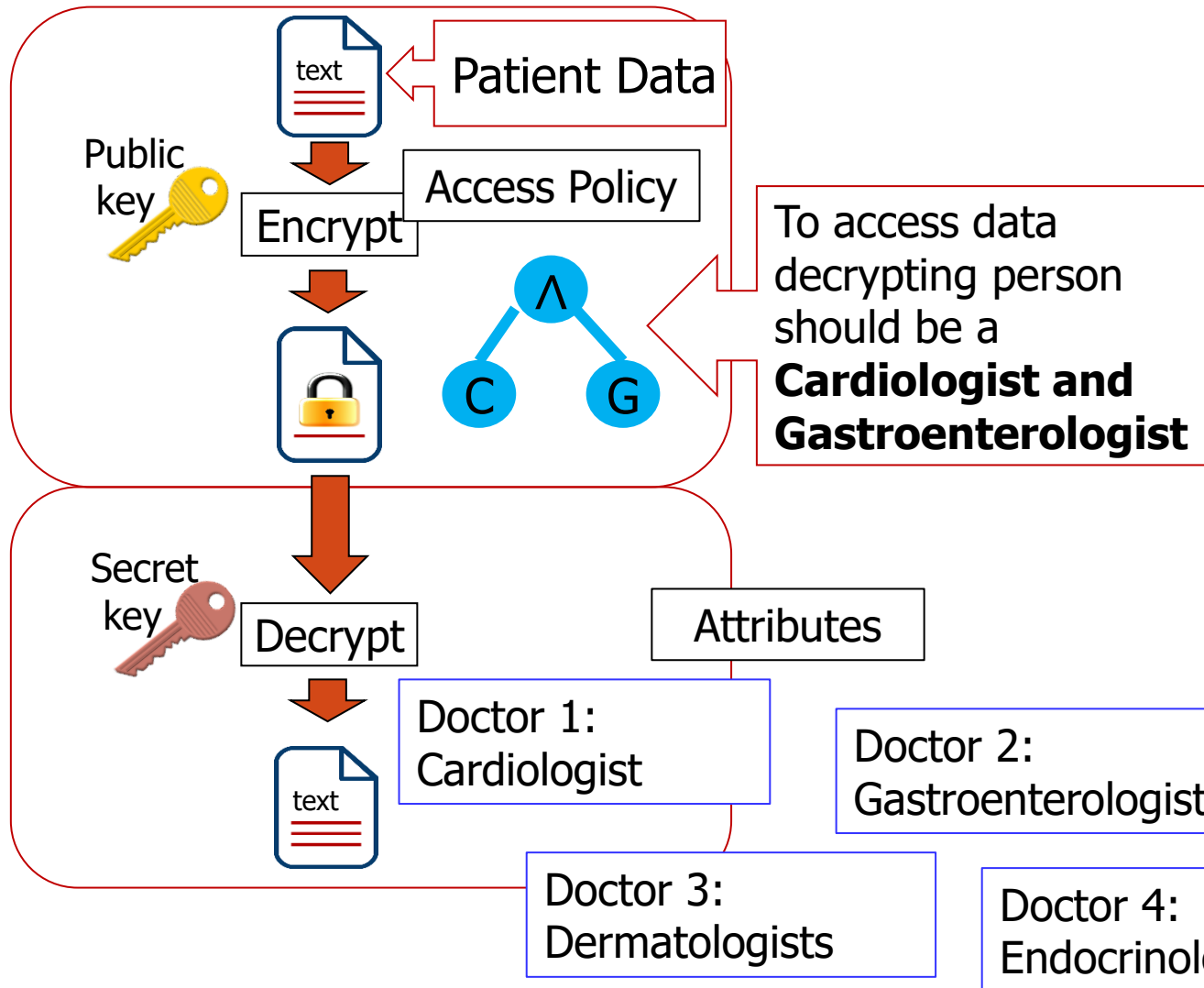




# CP-ABE Application – Patient Health Record System??

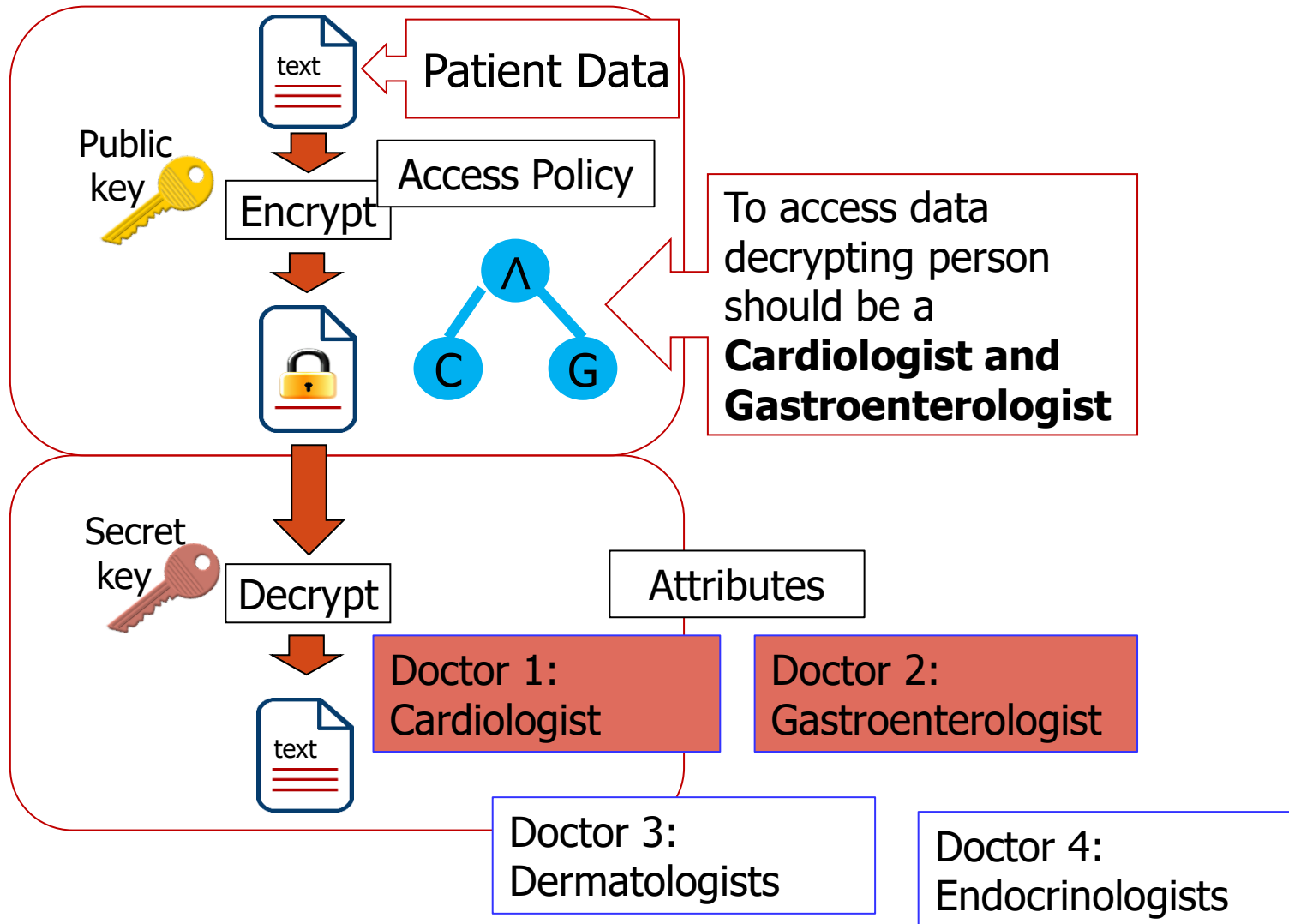


# Necessity of GO-ABE [Li et al. 2015]



Since any doctor cannot satisfy the Access Policy Patient's life is in danger

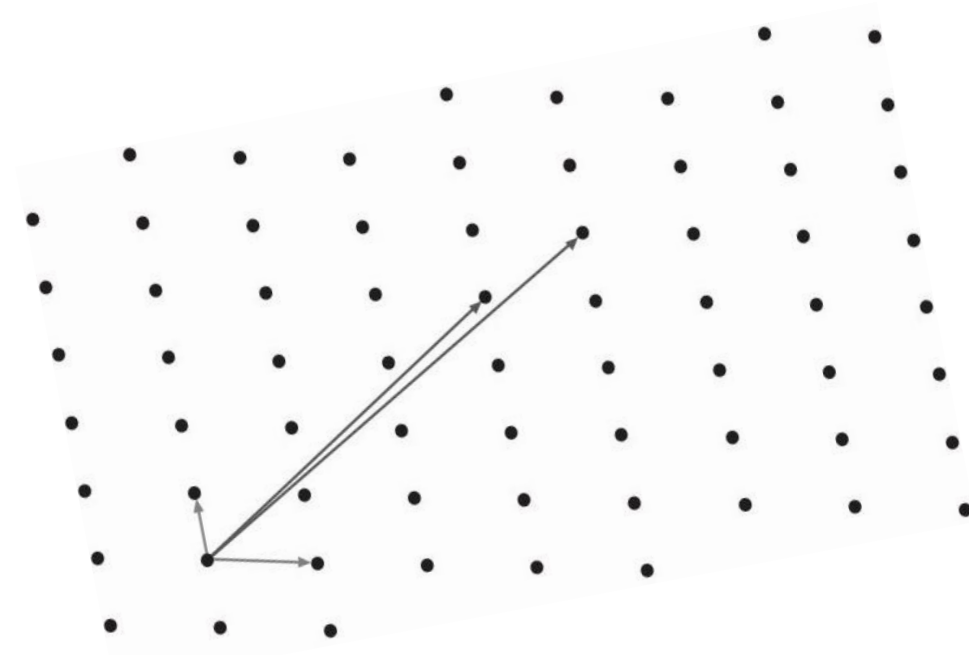
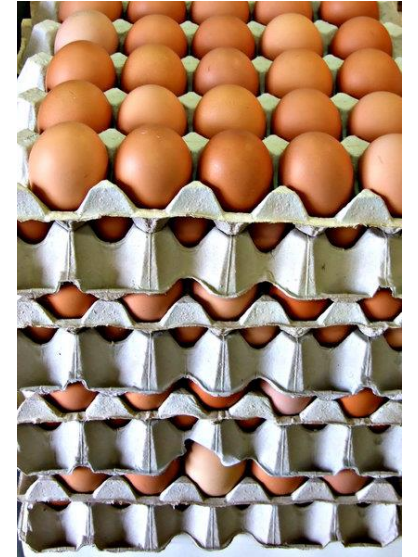
# Necessity of GO-ABE [Li et al. 2015]



Doctor 1 (**Cardiologist**) and Doctor 2 (**Gastroenterologist**) collaborate

- Even though both numerator and denominator in  $L_i$  can be bounded as a fraction of integers, when presenting Author Proof 6 M. N. S. Perera et al. as an element in  $\mathbb{Z}_q$  the value  $L_i$  is arbitrarily large. The idea of clearing the denominators prevents the large-value problem of  $L_i$ . Let  $D := (\frac{1}{2})^2$  be a sufficiently large constant, such that  $DL_i \in \mathbb{Z}$  for all  $i$ . Multiplying noise vectors of the encryption function with  $D$  we get,  $C_{id} = \text{IBE.Enc}(id, b \in \{0, 1\}) = (AT_1, id_1 s + De_1, \dots, AT_s, id_s + De_s, u^T s + De + bq/2)$ . Thus, it is sufficient to bound the below for the correctness of the IBE scheme by  $q/4$ .  $De_i - k \sum_{i \in S} DL_i x^T i e_i$  Since  $DL_i$  is an integer bounded by  $D^2$ , it is enough to select noise vectors bounded by  $q/4D$  with overwhelming probability.

# Lattices



Set of points in a n-dimension space, arrange on a periodical manner

